Scaling up Domain Agnostic Techniques for Program Synthesis

Théo Matricon

supervised by Nathanaël Fijalkow

université **BORDEAUX**



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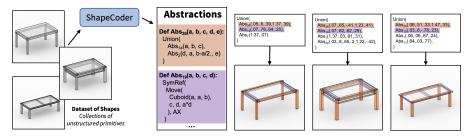
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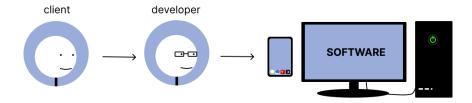
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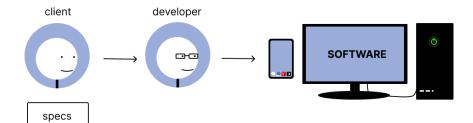
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5	Earlene McCarty	Earlene					and
6	Jon Voigt	Jon					and
7	Mia Arnold	Mia					
8	Jorge Fellows	Jorge					shows a
9	Rose Winters	Rose					
10	Carmela Hahn	Carmela					
11	Denis Horning	Denis					preview
12	Johnathan Swope	Johnatha					
13	Delia Cochran	Delia					
14	Marguerite Cervantes	Marguerit					
15	Liliana English	Liliana					
16	Wendy Stephenson	Wendy					

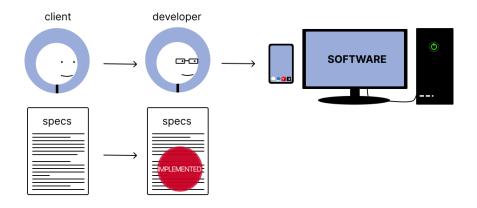
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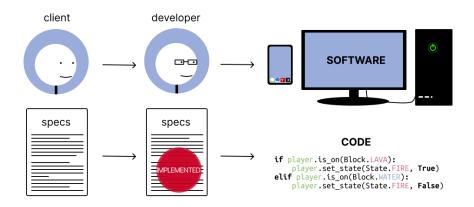


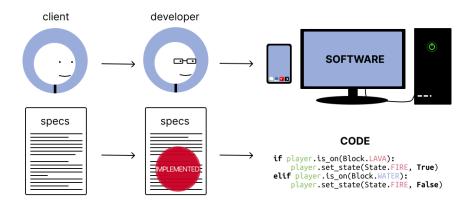
ShapeCoder [Jones et al., 2023]





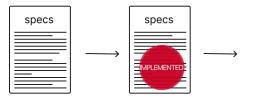






Can we assist developers with automatic code generation?

Program Synthesis



CODE

if player.is_on(Block.LAVA):
 player.set_state(State.FIRE, True)
elif player.is_on(Block.WATER):
 player.set_state(State.FIRE, False)

a deterministic tree grammar G

derivation rules are of the form: $S \rightarrow f \ S_1 \dots S_k$



Input:

- a deterministic tree grammar G : the search space
- a specification C that checks if a program p ∈ L(G) matches the specification

Output:

• a $p \in \mathcal{L}(G)$ such that $\mathcal{C}(p) = \checkmark$

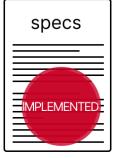
Logic: $\forall a, b$ $f(a, b) \ge a$ $f(a, b) \ge b$ $f(a, b) \in \{a, b\}$

Examples: f(1,5) = 5f(2,1) = 2f(-3,-9) = -3

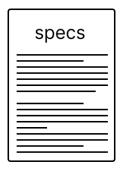
Natural language:

'Write a function that takes the maximum of its two arguments.'

Specifications



- Logic
- Examples



Natural Language

Relevant Articles of this thesis

Enumeration

- Fijalkow, Lagarde, Matricon, Ellis, Ohlmann, and Potta, *Scaling Neural Program Synthesis with Distribution-based Search*, 2022, AAAI
- Matricon, Fijalkow, and Lagarde, *Eco Search: A No-delay Best-First Search Algorithm for Program Synthesis*, 2025, AAAI

Others

- Matricon, Fijalkow, and Margueritte, *WikiCoder: Learning to Write Knowledge-Powered Code*, 2023, SPIN
- Matricon and Fijalkow, *Runtime Filtering: Semantic Pruning for Program Synthesis*, 2025, Under Preparation (to be submitted)

Software

• Matricon, Fijalkow, Lagarde, and Ellis, *DeepSynth: Scaling Neural Program Synthesis with Distribution-based Search*, 2022, Journal of Open Source Software

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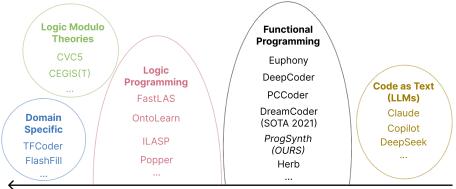
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Software

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Program Synthesis Frameworks



domain specific representations

Enumeration

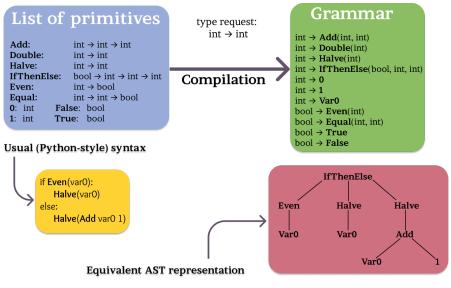
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Input:

- a deterministic tree grammar G : the search space
- a specification C that checks if a program p ∈ L(G) matches the specification

Output:

• a $p \in \mathcal{L}(G)$ such that $\mathcal{C}(p) = \checkmark$

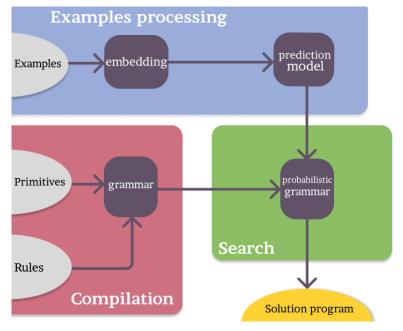


Basic If-Then-Else Grammar

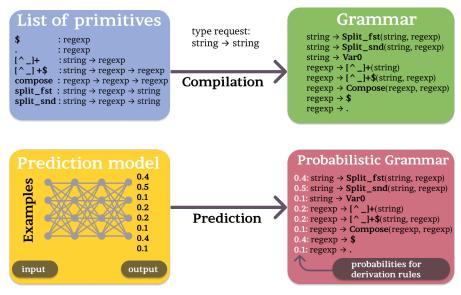
Symbolic search is not enough...

Symbolic search is not enough...

Enters machine learning [Balog et al., 2017]!



Our machine learning guided pipeline



Prediction Example

Enumeration Problem

Input: a probabilistic(weighted) deterministic tree grammar *G*

> **Goal**: enumerate all programs of *G*

BFS DFS Threshold [Menon et al., 2013] Sort and Add [Balog et al., 2017]

. . .

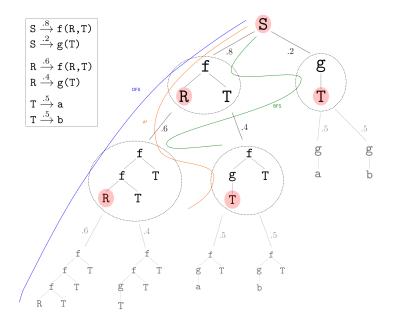
Input: a probabilistic(weighted) deterministic tree grammar *G*

Goal:

enumerate all programs of G in order of non-increasing probabilities

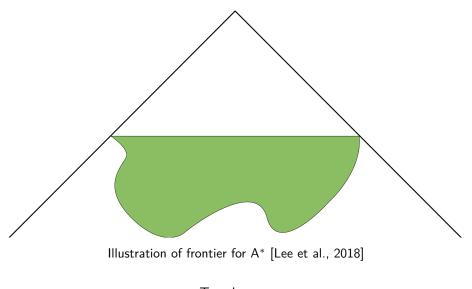
Delay:

time complexity between enumeration of the n^{th} program and the next



Time Comparison for a simple grammar with 3 non terminals

Best-first Search Algorithm	Time	Delay
A^* for program synthesis [Lee et al., 2018]	3h	$O(\log n)$
HEAPSEARCH [Fijalkow et al., 2022]	1h	$O(\log n)$
$\operatorname{BeeSearch}$ [Ameen and Lelis, 2023]	15min	$O(\log n)$
ECOSEARCH w/o buckets [Matricon et al., 2025]	11min	$O(\log n)$
ECOSEARCH [Matricon et al., 2025]	7min30	O(1)



- Top-down
- $O(\log n)$ delay

Key Idea: takes advantage of grammar structure

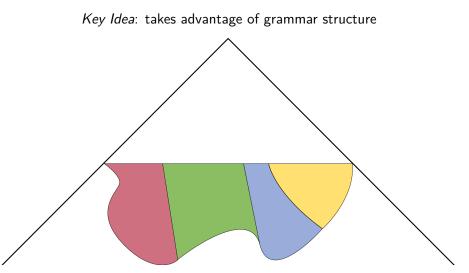
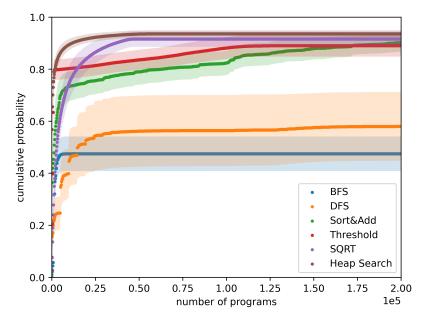


Illustration of frontier for HEAPSEARCH [Fijalkow et al., 2022]

- Bottom-up: fast evaluation + observational equivalence
- O(log n) delay

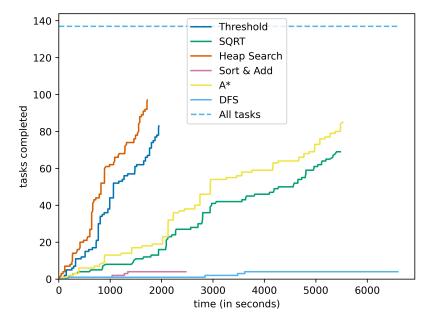


Cumulative probability w.r.t. number of programs enumerated

DeepCoder

integer list manipulation benchmark 500 tasks with programs of depth < 5 introduced in DeepCoder [Balog et al., 2017] simple grammar with 2 non terminals

```
def f(x: list[int]) -> list[int]:
    y = sort(x)
    return filter(is_even, y)
example = {
    input=[236, 147, -158, 99, 170],
    output=[-158, 17 0, 236]
}
```



Tasks solved using different enumeration algorithms on DeepCoder

Key Idea: structured frontier expansion

Key Idea: structured frontier expansion

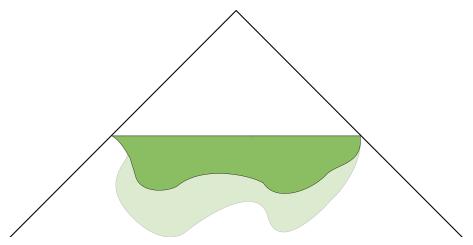


Illustration of frontier for BEESEARCH [Ameen and Lelis, 2023]

- Introduce cost tuple representation
- Better frontier expansion

Key Idea: unification of $\operatorname{HEAPSEARCH}$ and $\operatorname{BEESEARCH}$

Key Idea: unification of HEAPSEARCH and BEESEARCH

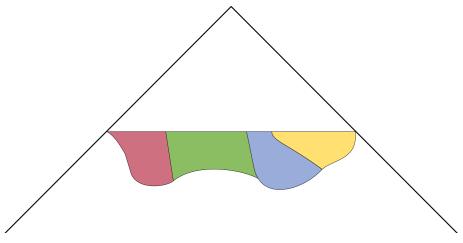
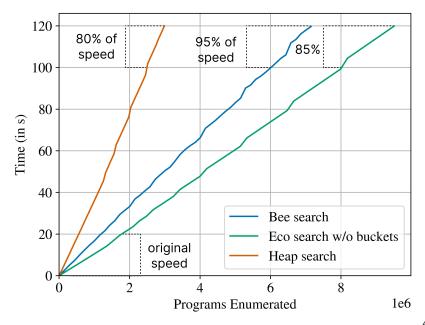


Illustration of frontier for ECOSEARCH without buckets [Matricon et al., 2025]

- $O(\log n)$ delay
- Frugal frontier expansion

Key Issue: $O(\log n)$ delay implies a slow-down over time

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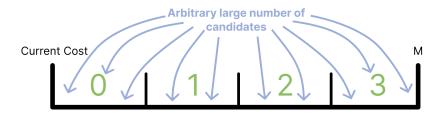
Key Theoretical Insight

There exists a constant $M \ge 0$ such that, for any program p and its successor p'we have $cost(p') - cost(p) \le M$.

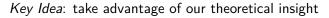
Key Theoretical Insight

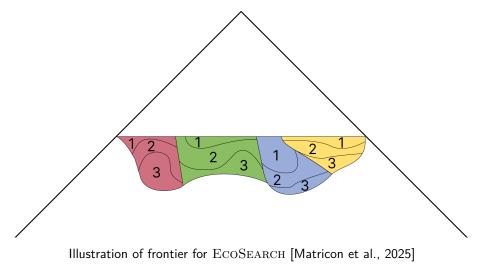
There exists a constant $M \ge 0$ such that, for any program p and its successor p'we have $cost(p') - cost(p) \le M$.

M does not depend on the number of programs enumerated.



Key Idea: take advantage of our theoretical insight



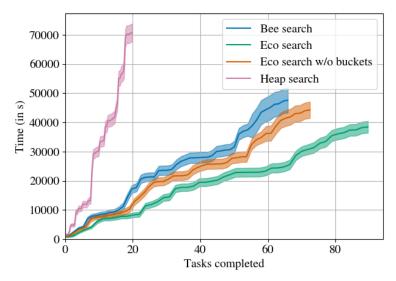


- O(1) delay
- Integer costs

FlashFill

string manipulation benchmark 100 tasks introduced in FlashFill [Gulwani, 2011] simple grammar with 3 non terminals

```
examples = [{
         input="736 miles",
        output="736"
    },
    Ł
         input="1255 miles",
         output = "1255"
    },
    ſ
         input="790 miles",
         output = "790"
    }
 ٦
```



Tasks solved using different enumeration algorithms on FlashFill

Conclusion

- From $O(\log n)$ top-down to $O(\log n)$ bottom-up
- From $O(\log n)$ bottom-up to O(1) bottom-up
- Faster program synthesis

But also (not mentioned)

- Introduced distribution-based search framework
- A "loss-optimal" sampling algorithm
- Grammar splitting to parallelise the search
- Better scaling with grammar complexity

Wikicoder

• Matricon, Fijalkow, and Margueritte, *WikiCoder: Learning to Write Knowledge-Powered Code*, 2023, SPIN

Paris \longrightarrow France code: 33 Berlin \longrightarrow Germany code: 49 Warsaw \longrightarrow Poland code: 48

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Syntactic processing cannot solve these tasks.

Paris \longrightarrow France code: 33 Berlin \longrightarrow Germany code: 49 Warsaw \longrightarrow Poland code: 48

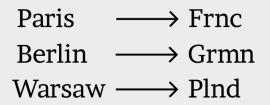
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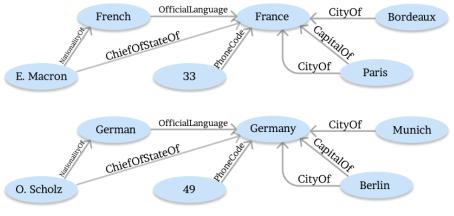
Syntactic Extraction

Semantic Processing

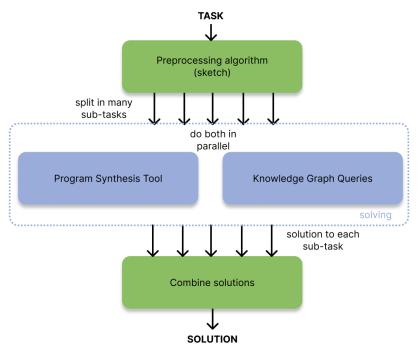
President Obama \longrightarrow Obama Prime Minister de Pfeffel Johnson \longrightarrow de Pfeffel Johnson

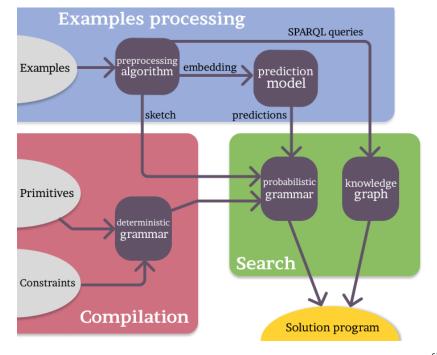
Knowledge Post-Processing

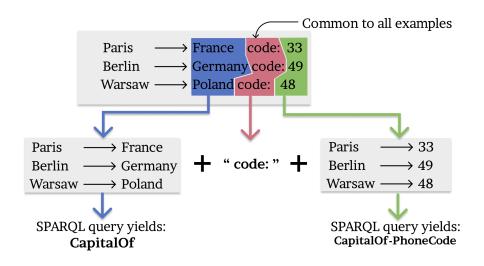


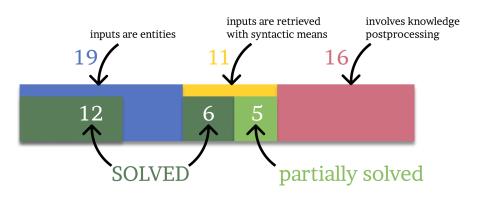


Idealized extract from YAGO/WikiData









- Different levels of knowledge in programs
- Tackled entities and syntactic extraction
- Strong hypothesis on the domain

Conclusion

- HEAPSEARCH: first $O(\log n)$ bottom-up
- ECOSEARCH: first O(1) and bottom-up
- Speed-up: A*: 3h ECOSEARCH: 7min30
- Knowledge-powered programs
- Different levels of complexity in knowledge-powered program synthesis
- Tackled entities and syntactic extraction

Conclusion

But also (not mentioned)

- Introduced distribution-based search framework
- A "loss-optimal" sampling algorithm
- Grammar splitting to parallelise the search
- Improved scaling of enumeration with grammar complexity
- Generate semantic equalities automatically
- Prune semantic redundant programs in O(1) at runtime

ProgSynth

Generic Synthesis Library

- 10k lines of code
- 2.5k lines of test

Programming By Examples Specific

8k lines of code

Perspectives

- How can we remove memory constraints of enumeration algorithms?
- How can we have GPU-friendly implementations?
- How can we parallelise program synthesis?
- How can we combine enumerative search paradigm with LLMs?
- And more generally, can we combine multiple paradigms?

Runtime Filtering

• Matricon and Fijalkow, *Runtime Filtering: Semantic Pruning for Program Synthesis*, 2025, Under Preparation

- 0+1 is useless: it does not use the input variable Var0;
- Ouble(Halve(P)) is redundant: it is equivalent to P;
- Add(Add(P,Q),R) and Add(P, Add(Q,R)) are equivalent
- Add(P,Q) and Add(Q,P) are equivalent.

- Var0 must be used at least once rules out the program 0+1;
- Ø Forbidding Double(Halve) rules out Double(Halve(P));
- Forbidding Add(_,Add) rules out programs associating addition to the right;
- Choosing between Add(P,Q) and Add(Q,P) would imply ordering all programs, which context-free grammars cannot do.

$B \Longrightarrow \operatorname{And}(B,B) \mid \operatorname{Or}(B,B) \mid \operatorname{Not}(B) \mid \operatorname{Var0} \mid \operatorname{Var1}$

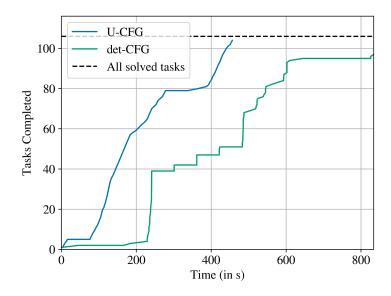
- $B_1 \implies \operatorname{And}(B_1, B_1) \mid \operatorname{Or}(B_2, B_2) \mid \operatorname{Not}(B_3) \mid \operatorname{Var0} \mid \operatorname{Var1}$
- $B_2 \implies \texttt{Or}(B_2, B_2) \mid \texttt{Not}(B_3) \mid \texttt{Var0} \mid \texttt{Var1}$
- $B_3 \implies Not(B_3) | Var0 | Var1$

- We enumerate all programs where each variable appears at most once, up to some fixed depth and some fixed number of variables;
- We check for program equivalence amongst all generated programs;
- For each equation found where one program is larger than the other one, we add a rule to forbid the larger program;

- The compilation of rules are performed on DBTAs.
- Minimisation are performed on DBTAs.
- Enumeration is performed on det-CFG and pruned by the DBTA.

Number of programs and respective proportions (prop.) with respect to maximum depth in the List Programming DSL with type 'int list \rightarrow int list'.

depth	no rules	with rules (prop.)
3	8.77e+04	0.83
4	3.34e+16	0.51
5	9.20e+52	0.13
6	4.79e+165	0.0015
7	4.14e+510	10^{-9}



Number of tasks solved with respect to cumulative time on the set of all solved List Programming tasks

- Find rules once and for all
- Compile the rules
- Almost-free pruning even with a smaller grammar model for bottom-up processes

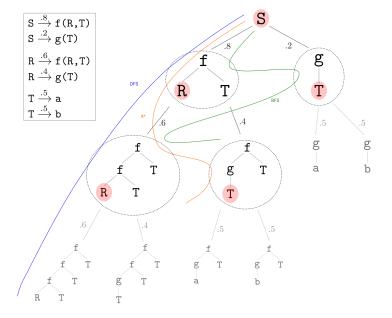
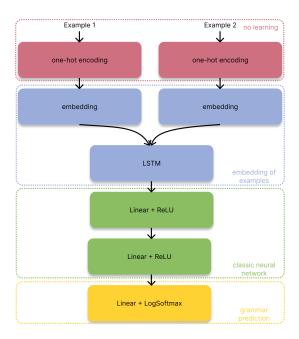
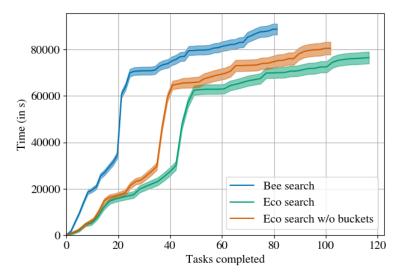


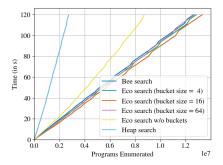
Illustration of the tree of leftmost derivations.

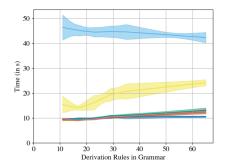


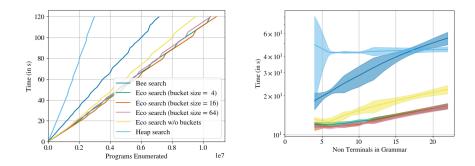
$\begin{array}{c} S \xrightarrow{.6} A \\ S \xrightarrow{.3} B \\ S \xrightarrow{.1} C \end{array}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c} S \xrightarrow{-1} C \\ S \xrightarrow{-1} D \\ A \xrightarrow{-1} E \\ A \xrightarrow{-3} F \\ A \xrightarrow{-2} H \\ B \xrightarrow{-5} I \\ B \xrightarrow{-5} J \\ E \xrightarrow{-1} \cdots \\ \vdots & \vdots & \vdots \end{array} $	$= .3 \times \begin{bmatrix} S \xrightarrow{1} A \\ A \xrightarrow{1} E \\ E \xrightarrow{2} \cdots \\ \vdots & \vdots & \vdots \end{bmatrix} + .28 \times \begin{bmatrix} S \xrightarrow{.857} A \\ S \xrightarrow{.143} C \\ A \xrightarrow{1} \xrightarrow{1} F \\ F \xrightarrow{2} \cdots \\ \vdots & \vdots & \vdots \end{bmatrix} + .27 \times \begin{bmatrix} S \xrightarrow{.667} A \\ S \xrightarrow{.333} B \\ A \xrightarrow{1} \xrightarrow{1} H \\ B \xrightarrow{1} \xrightarrow{1} I \\ H \xrightarrow{2} \cdots \\ \vdots & \vdots & \vdots \end{bmatrix} + .25 \times \begin{bmatrix} S \xrightarrow{.75} B \\ S \xrightarrow{.25} D \\ B \xrightarrow{1} \xrightarrow{1} J \\ J \xrightarrow{2} \cdots \\ \vdots & \vdots & \vdots \end{bmatrix}$

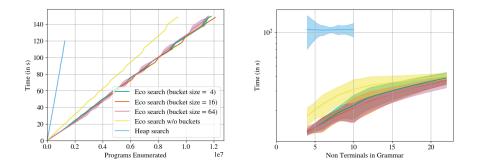


Tasks solved using different enumeration algorithms on DeepCoder









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